



# Unstructured Mesh Overview

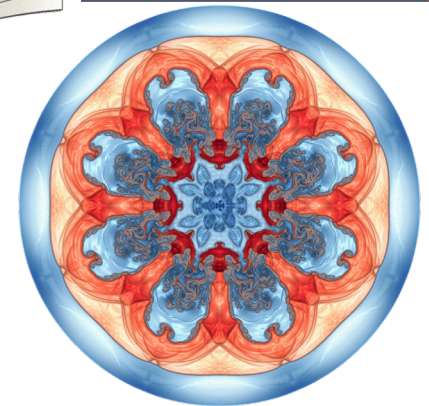
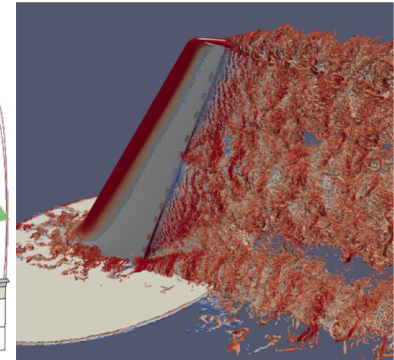
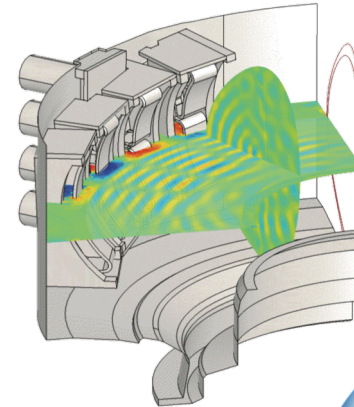
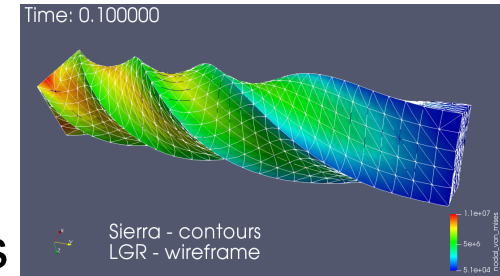
## Technical Leads

M. Adams (LBL), Karen Devine (Sandia), V. Dobrev (LLNL), D.A. Ibanez (SNL),  
K.E. Jansen (Colorado), M. Kneplay (Buffalo), T. Kolev (LLNL),  
O. Sahni (RPI), M.S. Shephard (RPI), C.W. Smith (RPI), G. Slota (RPI)



# Unstructured Mesh Analysis Codes

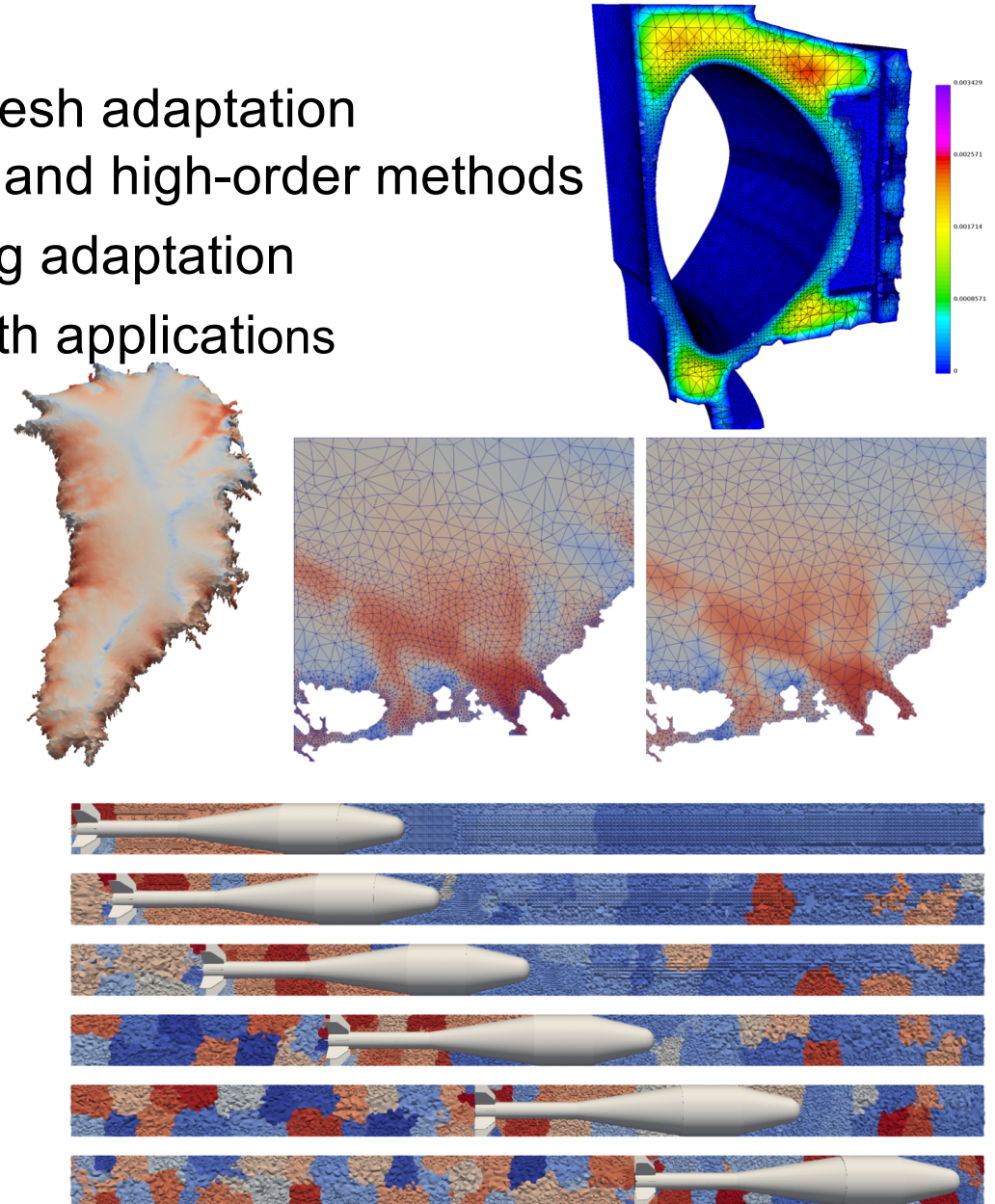
- FASTMath Activities
  - Develop unstructured mesh-based analysis tools
  - Demonstrate performance at full machine scale
  - Consider alternative equation discretization methods
  - Apply these analysis technologies towards applications
- Relevant Software Tools
  - MFEM – High Order F.E. Library
  - Albany/LGR – PDE solution application, large deformation mechanics
  - PHASTA – Navier-Stokes flow solver
- Applications Impacted
  - Fusion
  - Non-linear large deformation solid mechanics
  - Shock hydrodynamics
  - CFD applications



*Our unstructured mesh tools are used in many apps: from elasticity, to incompressible and compressible flows, and fusion*

# Unstructured Mesh Adaptation Technology

- FASTMath Activities
  - Provide parallel unstructured mesh adaptation technologies for both low order and high-order methods
  - Conforming and non-conforming adaptation
  - Integrate these technologies with applications
- Relevant Software
  - Omega\_h
  - MFEM
  - PUMI
  - MeshAdapt
- Applications Impacted
  - Albany/LGR for non-linear large deformation solid mechanics
  - M3D-C1, GITR, hPIC and XGC for Fusion for PIC codes
  - MFEM for Fusion, Flow, Elasticity and High-Order applications
  - PHASTA for CFD applications



# Performant Unstructured Meshes

## FASTMath Activities

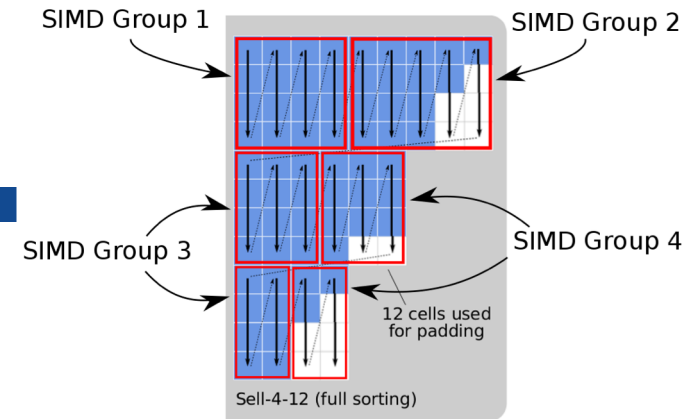
- Develop unstructured meshing technologies that execute on near exascale systems
- Support interactions between solvers and unstructured meshes
- Integrate these technologies into unstructured mesh simulation tools

## Relevant Software Tools

- Omega\_h, MFEM, PHASTA, EnGPar, PUMIpic

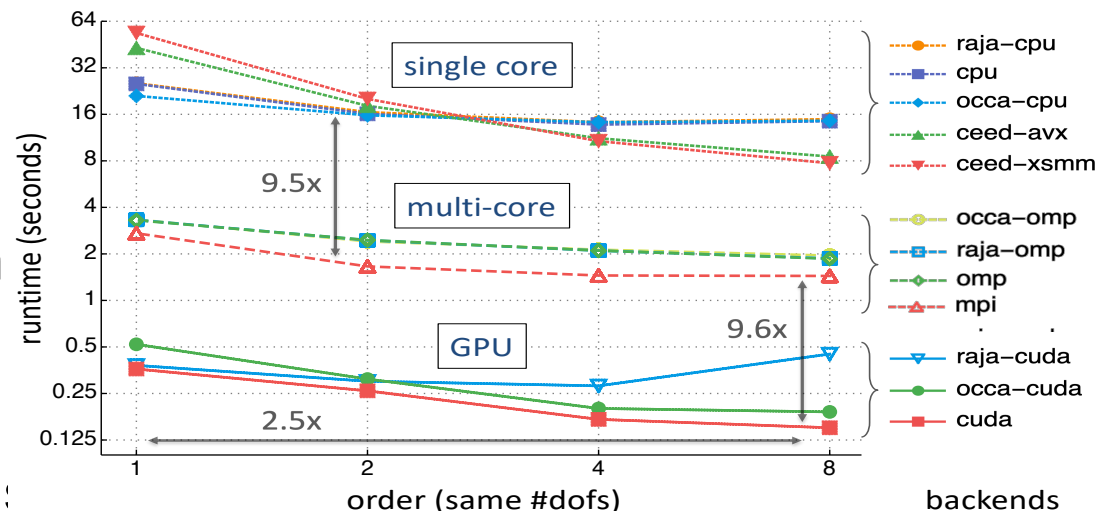
## Applications Impacted

- XGC, GITER & M3D-C<sup>1</sup>Fusion
- MFEM for Fusion and other applications
- PHASTA for CFD application
- Albany/LGR Non-linear large deformation solid mechanics



SCS for particles on mesh

Example 1, 200 CG-PA iterations, 2D, 1.3M dofs, GV100 + 32 core Xeon (Linux)



**Initial results with  
MFEM v4.0**



# FASTMath provides advanced dynamic load balancing and task mapping for extreme scale applications

## ■ FASTMath Activities

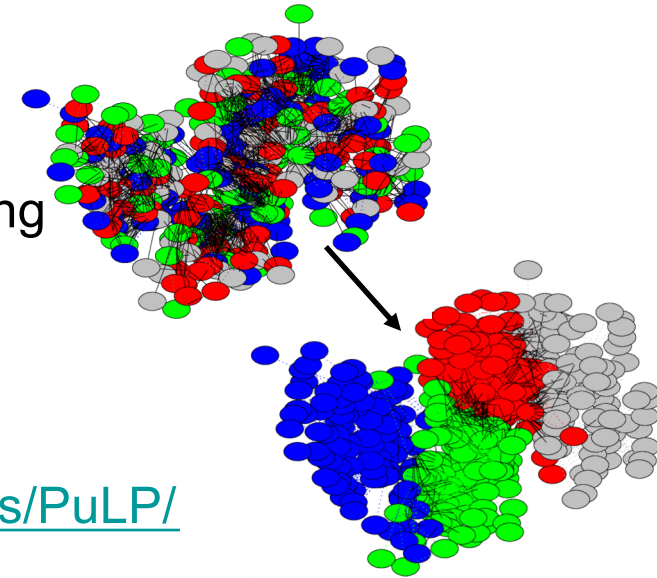
- Massively parallel graph algorithms
- Architecture aware load balancing and task mapping
- Multi-criteria dynamic partition improvement

## ■ Relevant Software Tools

- PuLP and XtraPuLP: Graph Partitioning using Label Propagation - [github.com/HPCGraphAnalysis/PuLP/](https://github.com/HPCGraphAnalysis/PuLP/)
- Zoltan and Zoltan2 - [www.cs.sandia.gov/zoltan/](http://www.cs.sandia.gov/zoltan/)
- EnGPar – [scorec.github.io/EnGPar/](https://scorec.github.io/EnGPar/)

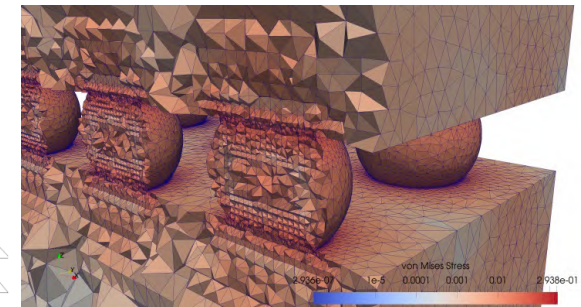
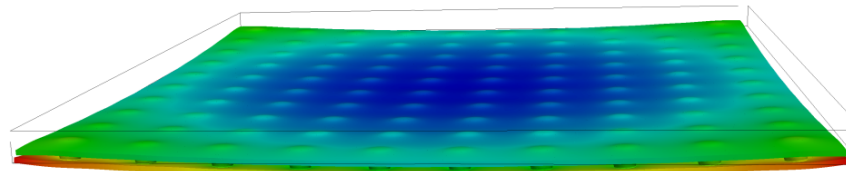
## ■ Applications Impacted

- Albany Multiphysics
- XGC, GITR – fusion
- MFEM
- E3SM HOMME
- NNSA Sierra



The XtraPuLP graph partitioner can compute balanced multi-object partitionings of irregular trillion-edge graphs in minutes

Error-driven in-memory mesh adaptation of thermal creep in a flip-chip using Albany Multiphysics and Zoltan



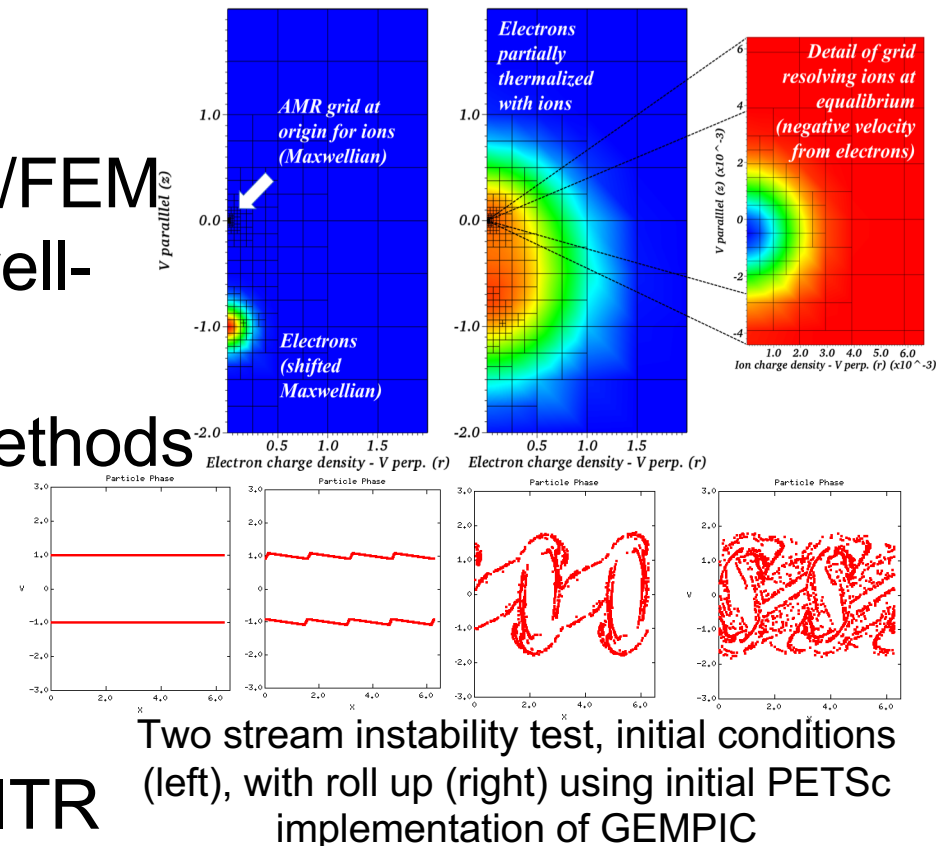
# Unstructured Mesh Methods for Particle in Cell Simulations

## ■ FASTMath Activities

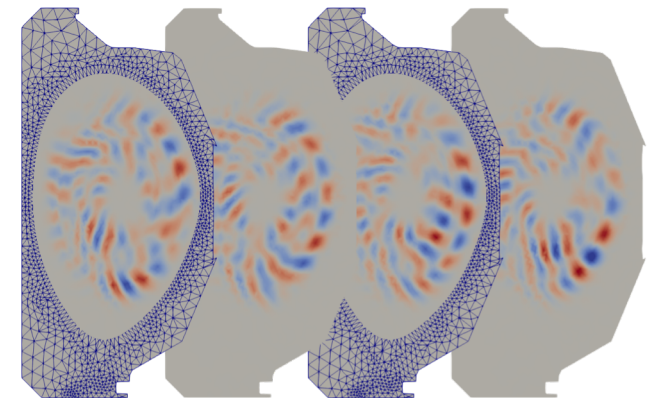
- Conservative coupled particle/FEM method for the Vlasov-Maxwell-Landau system
- Parallel unstructured mesh methods for PIC simulation codes

## ■ Applications Impacted

- Fusion Edge Plasma – XGC
- Fusion impurity modeling – GITR
- Core Plasma – GEMPIC, M3D-C1pic

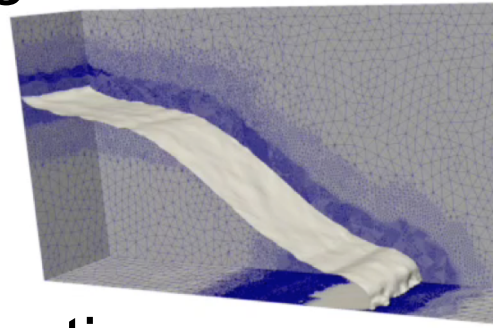


Snapshot of electrostatic potential fluctuation at toroidal angle  $\zeta=0, \pi/2, \pi, 3\pi/2$  from left to right for mesh-based XGC

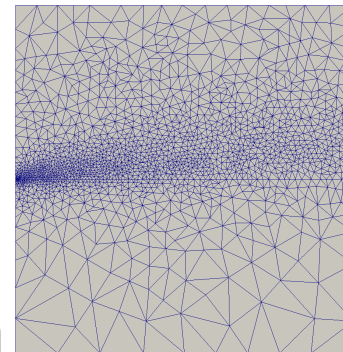


# Data Analytics for Unstructured Meshes

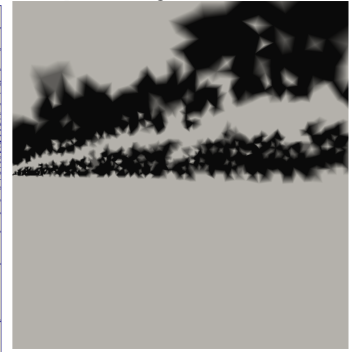
- Extraction of reliable engineering predictions and fundamental insights from simulations becomes challenging when:
  - Geometry is complex and evolving (e.g., physics-driven)
  - Discretization is large (even with adaptivity)
  - Number of input parameters is high (for design and UQ)
- FASTMath Activities
  - Unstructured mesh management
  - Computational steering
  - Multi-fidelity modeling
  - In situ visualization
- Applications Impacted
  - Flow applications
  - Plasma surface interactions



Joint adaptivity



Adapted mesh



Adapted order



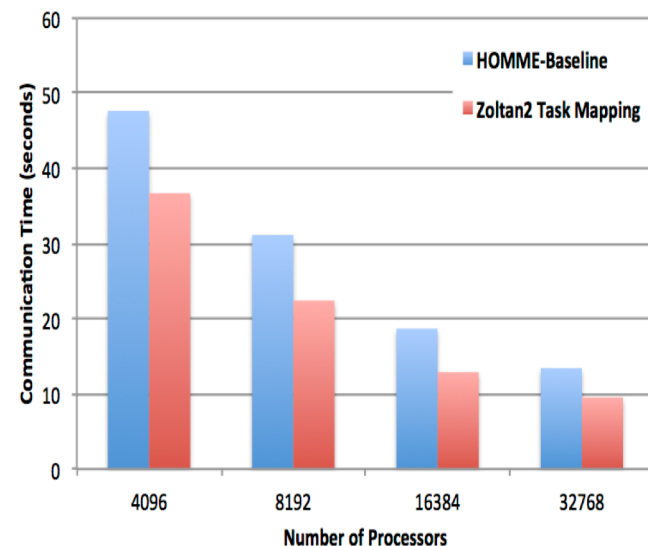
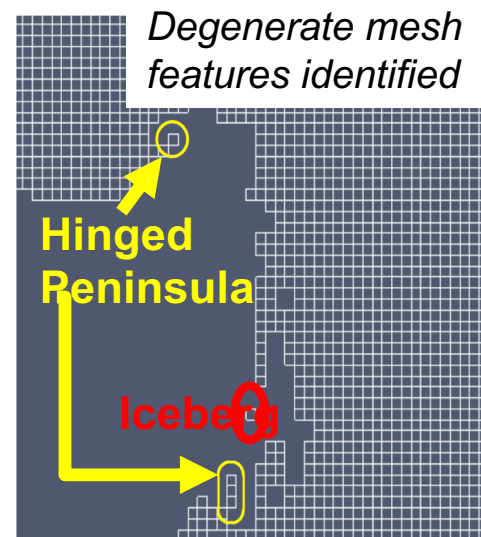
Expectation



Variance

# SciDAC ProSPeCT, E3SM and Zoltan2: Graph Algorithms, Task Mapping, and Partitioning

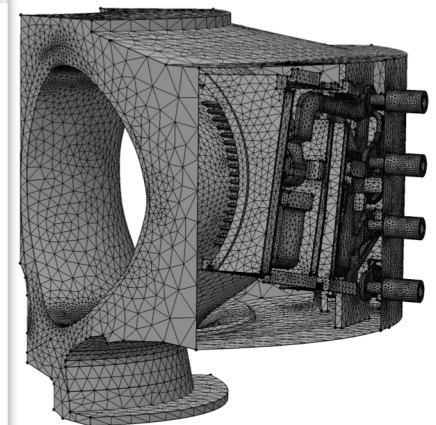
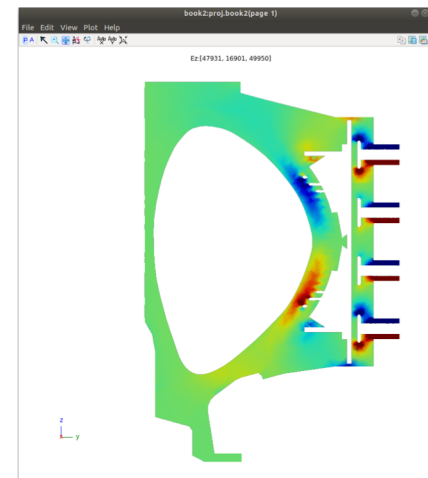
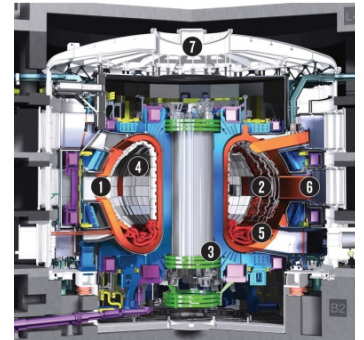
- Graph Algorithms for SciDAC ProSPeCT Ice Sheet Modeling
  - Algorithms developed to identification degenerate mesh features
  - Zoltan2's biconnected-component algorithms reduce time for degenerate mesh feature detection
- HOMME: High-Order Method Modeling Environment for atmospheric modeling
  - Unstructured quadrilateral meshes on the sphere
  - Zoltan2's geometric task placement reduces HOMME's communication time
- Partitioning in E3SM Climate Component Coupler
  - Zoltan's multi-weight geometric partitioners spatially align meshes so that little communication is needed during search and transfer





# Fusion SciDAC Unstructured Mesh Needs

- Unstructured mesh technologies for four fusion SciDACs
  - Center for Tokamak Transient Simulations, Steve Jardin, PPPL
  - High-fidelity Boundary Plasma Simulation, C.S. Chang
  - Int. Simulation of Fusion Relevant RF Actuators, Paul Bonoli, MIT
  - Plasma Surface Interactions, Brian Wirth, ORNL
- Unstructured mesh capabilities being provided
  - Combined physical and physics model entities
  - CAD model simplification
  - Mesh generation with specific mesh controls
  - Adaptive simulation workflows
  - Analysis code mesh infrastructure including assembly
  - Parallel mesh based PIC methods for three PIC codes



MFEM Result z-component of electric field on a x-plane cut view (1M ele.)

# Unstructured Mesh Collaborations

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- Within FASTMath
  - Solvers – Supporting mesh-based analysis codes
  - UQ – Unstructured meshes for UQ, UQ with adapted mesh
  - DATA – in situ data analytics
- With Rapids
  - In situ visualization and data methods
  - Performance of mesh adaptation
  - Methods to more effectively execute workflows
- With ECP (taking advantage of ECP developments)
  - CEED co-design center exascale discretizations
  - Fusion WDM application – coupling strategies
  - COPA co-design center for particle applications

## Summary of Posters:

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- Unstructured Mesh Analysis Codes
- Unstructured Mesh Adaptation
- Performant Unstructured Mesh Technologies
- Dynamic Load Balancing and Task Mapping for Extreme-Scale Dynamic Applications
- Unstructured Mesh Methods for Particle in Cell Simulations
- Data Analytics for Unstructured Meshes
- SciDAC ProSPecT, E3SM and Zoltan2: Graph Algorithms, Task Mapping, and Partitioning
- Unstructured Mesh Technologies for the Fusion SciDAC Centers